Sustained Slow-Scale Oscillation in Higher Order Current-Mode Controlled Converter

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Abstract—DC–DC converters under current-mode control have been known to exhibit slow-scale oscillation as a result of a Hopf-type bifurcation as one or more of the parameters of the outer voltage loop are varied. In the absence of the outer voltage loop (i.e., open loop), slow-scale oscillation was generally not observed in simple low-order dc–dc converters, i.e., buck, buck–boost, and boost converters. In this paper, slow-scale bifurcation in a higher order current-mode controlled converter is studied. It has been found experimentally that, even in the absence of a closed outer voltage loop, a current-mode controlled Ćuk converter can exhibit a slow-scale Hopf-type bifurcation. The phenomenon was observed in a commercial low-ripple dc–dc converter which has been designed using the Ćuk converter and the LM2611 controller. Such slow-scale oscillation of the inner current loop can also be observed in full-circuit SPICE simulations. An averaged model has been developed and implemented in SPICE to find the Hopf bifurcation boundaries. With this averaged model, the Hopf bifurcation can be explained conveniently using the traditional loop gain analysis. Specifically, the extra degrees of freedom in higher order dc–dc converters have opened up a new possible mode of instability which has not been found in simple low-order dc–dc converters.

Index Terms—Bifurcation, dc–dc converters, Ćuk converter, current-mode control.

I. INTRODUCTION

CURRENT-PROGRAMMED control, which is one of the most commonly used control schemes in dc–dc converters, has received much attention from power electronics practitioners in the past two decades [1], [2]. Recently, some nonlinear phenomena in current-mode controlled dc–dc converters have been studied [3], [4]. Generally, two distinct types of bifurcations have been identified, namely, slow-scale Hopf-type bifurcation and fast-scale bifurcation. The former can be regarded as a kind of low-frequency phenomenon which is caused by the voltage feedback loop permitting low-frequency oscillation [5]–[8]. The latter, however, is related to the inner current loop instability, and often manifests as period doubling at the switching frequency, as reported in [9], [10]. In particular, the outer voltage loop, through which low-frequency oscillation is sustained, has been found crucial to the occurrence of slow-scale Hopf-type bifurcation in current-mode controlled simple low-order dc–dc converters.

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Higher order dc–dc converters, such as the Ćuk converter, enable low ripple voltage and low rms current on both the input and the output sides. This is a significant advantage over other inverting topologies such as the buck–boost and flyback converters. For such higher order dc–dc converters under current-mode control, fast-scale bifurcation has been reported and analyzed [12], [13]. Previous studies have also suggested that, in the presence of the inner current loop, fast-scale period-doubling bifurcation occurs under variation of some parameters. However, slow-scale bifurcation is expected in the presence of an unstable outer voltage loop, which is consistent with results reported so far regarding slow-scale bifurcation of simple low-order dc–dc converters. In this paper, we will focus on an instability phenomenon, which has apparently been ignored in all past studies. Our initial observation was made from a commercial low-ripple dc–dc converter, the design of which has been based on a Ćuk converter and the use of the LM2611 controller for output regulation. The system's inner current loop has been compensated to avoid fast-scale bifurcation. It has been observed that slow-scale Hopf-type bifurcation occurs as the equivalent reference current is increased, even in the absence of a closed outer voltage loop, i.e., with the outer voltage loop opened. Moreover, with the outer voltage loop closed, one would still expect the system to become unstable, as in all previous studies of inner loop stability for simple low-order converters.

Our study in this paper will consist of the following aspects: 1) experimental observation of slow-scale bifurcation in the Ćuk converter controlled by the LM2611 controller with the outer voltage feedback loop opened; 2) full-circuit SPICE simulations confirming that the oscillation has been originated from the inner current loop; 3) development of an averaged model for analysis; 4) identification of the slow-scale bifurcation boundaries; and 5) derivation of stability boundaries analytically and verification by full-circuit SPICE simulations.

II. CURRENT-MODE CONTROLLED ĆUK CONVERTER

Fig. 1(a) shows the schematic diagram of a Ćuk converter under current-mode control. Unlike other simple low-order converters, the Ćuk converter can operate in continuous conduction mode (CCM) and a number of discontinuous conduction modes [14]. At present, the dynamics of the Ćuk converter remains relatively unexplored, even for the simplest CCM operation. For simplicity, we will focus on operation in CCM, for which only two complimentary switch states are involved, i.e., the switch is closed while the diode is open, and *vice versa*. Provided that the sum of the inductor currents $i_1 + i_2$ remains positive, the diode conducts current for the whole subinterval during which the switch is off, and the Ćuk converter maintains in CCM. Specifically, the sum of the inductor currents is the programming variable which, by comparing with the difference of the reference

Fig. 1. (a) Current-mode controlled Ćuk converter with the outer voltage loop opened. (b) Practical circuit with LM2611 controller.

Fig. 2. Waveform of $i_1 + i_2$ in current-mode controlled Ćuk converter.

current I_{ref} and the compensation current dI_{comp} , generates the on-off driving signal for the switch, where d is the duty cycle. Switch S is turned on by the clock signal at the beginning of the switching period T , i.e., at $t = nT$ for integer n . The inductor currents i_1 and i_2 ramp up. As $i_1 + i_2$ climbs to the value of $I_{ref} - dI_{comp}$, switch S is turned off and remains off until the next cycle begins. A typical waveform of $i_1 + i_2$ is shown in Fig. 2.

The problem of fast-scale period-doubling bifurcation in this type of converter circuits has been widely documented [12], [13]. Specifically, the inner current loop has been identified as the main structural cause of the observed period-doubling bifurcation. In the absence of the compensation ramp, the onset of period doubling occurs when the duty cycle exceeds 0.5. The use of a compensation ramp, as described in Fig. 2, would stabilize the inner current loop in the sense that the critical value of the duty cycle is extended beyond 0.5.

TABLE I
COMPONENT VALUES USED IN EXPERIMENT

Circuit Components	Values
Input Voltage E	3.9 V
Inductance L_1	10 μ H
Inductance L_2	10 μ H
Capacitance C_C	1 μ F
Capacitance C_O	20 μ F
Load Resistance R	25 Ω

Fig. 3. Experimental slow-scale oscillations in the current-mode controlled Ćuk converter using LM2611. Upper trace: i_1 (200 mA/div); lower trace: i_2 (200 mA/div). Time scale is 10 μ s/div.

TABLE II
OTHER COMPONENT VALUES ESTIMATED AND USED IN SIMULATIONS

Circuit Components	Values
Switching Frequency f	700 kHz
Resistance r_1	0.73 Ω
Resistance r_2	0.20 Ω
I_{ref}	2.7 A
I_{comp}	1 A

III. EXPERIMENTS AND COMPUTER SIMULATION STUDY

We have built a Ćuk converter with LM2611, as shown in Fig. 1(b). The component values are given in Table I. Oscillatory waveforms have persistently been observed, as shown in Fig. 3, for the two inductor currents while the voltage feedback pin of LM2611 has been disconnected.

In order to confirm that the oscillation is caused by the current-loop instability rather than circuit noises or other coupling effects, we have performed SPICE simulations under an ideal circuit environment. Table II shows the additional parameters used in simulation. The switching frequency used is the same as that observed from the experimental current waveforms. The equivalent resistances r_1 and r_2 are estimated from the data sheets of LM2611 and the components used. The corresponding simulated inductor current waveforms are shown in Fig. 4 for $I_{ref} = 2.7$ A and $I_{comp} = 1$ A. We observe that the simulated and experimental waveforms are in good agreement.

As we are interested in the low-frequency behavior of the circuit, it suffices to use an averaged model for capturing low-frequency dynamics. Fig. 5 shows such a model for the Ćuk converter under study [11]. This model retains the essential low-frequency behavior, although high-frequency details would have been discarded by the averaging process. Thus, the averaged model is still expected to capture the slow-scale oscillations, as

Fig. 4. Full-circuit SPICE simulated waveforms of i_1 (upper trace) and i_2 (lower trace) for the current-mode controlled Ćuk converter using LM2611 controller. Component values are given in Tables I and II.

Fig. 6. SPICE averaged model simulated waveforms of i_1 (upper trace) and i_2 (lower trace) for the current-mode controlled Ćuk converter using LM2611 controller. Component values are given in Tables I and II.

Fig. 5. SPICE averaged model for the current-mode controlled Ćuk converter. Component values are given in Tables I and II. Expressions for dependent sources are: $i_{1m} = i_1$, $i_C = (1-d)i_1 - di_2$, $i_O = i_2$, $d = v_d$, $v_1 = E - (1-d)v_C$, $v_2 = dv_C - v_O$, $I_{off} = (dT)/(2)((E - i_1 r_1)/(L_1) + (v_C - v_O - i_2 r_2)/(L_2)) - dI_{comp}$, and $v_d = (v_{L1} + v_O)/(E - v_{L2} + v_O)$.

confirmed by the simulated waveforms shown in Fig. 6 for circuit parameters given in Tables I and II.

IV. THEORETICAL ANALYSIS OF SLOW-SCALE BIFURCATION BEHAVIOR

From the foregoing experimental and simulation studies, we have observed current-loop induced Hopf bifurcation. Here, we will use the averaged model to analyze the bifurcation phenomenon and to locate the bifurcation boundary useful for design purposes.

First, we write the set of averaged equations describing the Ćuk converter as follows:

$$\begin{cases} i_1' = -\frac{(1-d)v_C}{L_1} - \frac{i_1 r_1}{L_1} + \frac{E}{L_1} \\ i_2' = \frac{-v_O + dv_C}{L_2} - \frac{i_2 r_2}{L_2} \\ v_O' = \frac{i_2}{C_O} - \frac{v_O}{C_O R} \\ v_C' = \frac{(1-d)i_1}{C_C} - \frac{di_2}{C_C} \end{cases} \quad (1)$$

where prime ($'$) denotes time derivative, and d is the duty cycle which is the fraction of the switching period T for which the switch S is turned on.

By inspection of the circuit [Fig. 1(a)] and the waveforms (Fig. 2), the average value of $i_1 + i_2$ can be expressed as

$$i_1 + i_2 = I_{ref} - \frac{dT}{2} \left(\frac{E - i_1 r_1}{L_1} + \frac{v_C - v_O - i_2 r_2}{L_2} \right) - dI_{comp} \quad (2)$$

It is assumed that the system is free from fast-scale current-loop instability as a result of proper application of current loop compensation, and in particular the amount of compensation is given by

$$I_{comp} = \frac{d-0.5}{1-d} ET \left(\frac{1}{L_1} + \frac{1}{L_2} \right). \quad (3)$$

We now take the Fourier series expansion of every state variable. In general, variable $x(t)$ can be expanded as

$$x(t) = \mathbf{x}_0 + \mathbf{x}_1 \exp(j\omega t) + (\mathbf{x}_1 \exp(j\omega t))^* + \sum_{n=2}^{\infty} [\mathbf{x}_n \exp(jn\omega t) + (\mathbf{x}_n \exp(jn\omega t))^*] \quad (4)$$

where superscript $*$ denotes complex conjugation, $\omega = 2\pi f$ denotes the fundamental frequency of oscillation, and $\mathbf{x}_n$ is the n th harmonic component of $x(t)$ which is given by

$$\mathbf{x}_n = x_{nr} + jx_{ni} = \frac{\omega}{2\pi} \int_{t-\frac{2\pi}{\omega}}^t x(\tau) \exp(-jn\omega\tau) d\tau. \quad (5)$$

Here, the dot product of two complex numbers, $\mathbf{x}_n$ and $\mathbf{y}_n$, can be defined as $\mathbf{x}_n \cdot \mathbf{y}_n = x_{nr}y_{nr} + x_{ni}y_{ni}$. Suppose $\mathbf{d}_n$, $\mathbf{v}_{Cn}$, $\mathbf{i}_{1n}$

Fig. 7. Stability boundaries for different values of loading resistance: upper line for $R = 25 \Omega$, middle line for $R = 20 \Omega$, and bottom line for $R = 15 \Omega$. Points are boundaries found from full-circuit simulations. Unstable and stable regions of operation are located above and below the line, respectively.

and $\mathbf{i}_{2n}$ are the n th components of d, v_C, i_1 and i_2 . Using (4) and (5), (1) becomes

$$\begin{cases} L_1 i'_{10} = -(1-d_0)v_{C0} + 2\mathbf{d}_1 \cdot \mathbf{v}_{C1} - i_{10}r_1 + E \\ L_2 i'_{20} = -v_{O0} + d_0v_{C0} + 2\mathbf{d}_1 \cdot \mathbf{v}_{C1} - i_{20}r_2 \\ C_O v'_{O0} = i_{20} - \frac{v_{O0}}{R} \\ C_C v'_{C0} = (1-d_0)i_{10} - d_0i_{20} - 2\mathbf{d}_1 \cdot (\mathbf{i}_{11} + \mathbf{i}_{21}) \end{cases} \quad (6)$$

$$\begin{cases} L_1 i'_{11} + j\omega L_1 i_{11} = -(1-d_0)v_{C1} + d_1v_{C0} - i_{11}r_1 \\ L_2 i'_{21} + j\omega L_2 i_{21} = -v_{O1} + d_0v_{C1} + d_1v_{C0} - i_{21}r_2 \\ C_O v'_{O1} + j\omega C_O v_{O1} = i_{21} - \frac{v_{O1}}{R} \\ C_C v'_{C1} + j\omega C_C v_{C1} = i_{11} - d_0(i_{11} + i_{21}) - (i_{10} + i_{20})d_1 \end{cases} \quad (7)$$

for $n = 0$ and 1 , respectively. Similarly, (2) becomes

$$\begin{aligned} i_{10} + i_{20} &= I_{\text{ref}0} \\ &\quad - d_0 \frac{T}{2} \left(\frac{E - i_{10}r_1}{L_1} + \frac{v_{C0} - v_{O0} - i_{20}r_2}{L_2} \right) \\ &\quad - T\mathbf{d}_1 \cdot \left(-\frac{\mathbf{i}_{11}r_1}{L_1} + \frac{\mathbf{v}_{C1} - \mathbf{v}_{O1} - \mathbf{i}_{21}r_2}{L_2} \right) \\ &\quad - d_0 I_{\text{comp}} \end{aligned} \quad (8)$$

$$\begin{aligned} i_{11} &\left(1 - \frac{d_0 T}{2} \frac{r_1}{L_1} \right) + d_0 \frac{T}{2} \frac{v_{C1}}{L_2} \\ &\quad + i_{21} \left(1 - \left(\frac{R}{1 + j\omega C_O R} + r_2 \right) \frac{d_0 T}{2L_2} \right) \\ &= I_{\text{ref}1} - d_1 I_{\text{comp}} \\ &\quad - d_1 \frac{T}{2} \left(\frac{E - i_{10}r_1}{L_1} + \frac{v_{C0} - v_{O0} - i_{20}r_2}{L_2} \right) \end{aligned} \quad (9)$$

Equations (6) and (8) describe the dynamics of the dc components while (7) and (9) give the dynamics of the fundamental frequency components for the system. To test the stability of the

system, we first calculate the steady-state solutions of dc components from (6) and (8) and the fundamental components from (7) and (9) for the system. The loop gain at the fundamental frequency will be calculated using the steady-state solution of (7) and (9). The stability of the system can then be tested using the Barkhausen criteria.

The steady-state solution of dc components can be obtained by setting all time-derivatives in (6) to zero and solving for i_{10}, i_{20}, v_{C0} and v_{O0} . This gives

$$\begin{cases} v_{C0} = \frac{(1-d_0)(R+r_2)E - r_1(R+r_2)G}{\Delta} + \frac{[(1-d_0)(R+r_2) - d_0r_1]F}{\Delta} \\ i_{10} = \frac{d_0^2 E + d_0 F + (1-d_0)(R+r_2)G}{\Delta} \\ i_{20} = \frac{d_0(1-d_0)E + (1-d_0)F - d_0r_1G}{\Delta} \\ v_{O0} = i_{20}R \end{cases} \quad (10)$$

where $\Delta = (1-d_0)^2(R+r_2) + d_0^2 r_1$, $F = 2\mathbf{d}_1 \cdot \mathbf{v}_{C1}$ and $G = 2\mathbf{d}_1 \cdot (\mathbf{i}_{11} + \mathbf{i}_{21})$. Therefore, d_0 , before the system enters the instability region, can be found by putting (10) into (8) and assuming nearly zero fundamental component magnitudes, i.e., $F \approx 0$ and $G \approx 0$.

The fundamental components at steady state can be obtained by setting all derivatives to zero in (7), giving

$$\begin{cases} (j\omega L_1 + r_1)i_{11} = -(1-d_0)v_{C1} + v_{C0}d_1 \\ (j\omega L_2 + r_2)i_{21} = -v_{O1} + d_0v_{C1} + v_{C0}d_1 \\ (j\omega C_O + \frac{1}{R})v_{O1} = i_{21} \\ j\omega C_C v_{C1} = (1-d_0)i_{11} - d_0i_{21} - (i_{10} + i_{20})d_1 \end{cases} \quad (11)$$

The transfer functions $H_{v_C} \equiv v_{C1}/d_1$ of the converter and $H_d \equiv d_1/v_{C1}$ of the current programming function can be obtained by eliminating i_{11}, i_{21} and v_{O1} from (11) and (9), respectively. We thus have

$$\begin{aligned} H_{v_C} &= \frac{v_{C1}}{d_1} \\ &= \frac{-d_0v_{C0}X_1 + (1-d_0)v_{C0}X_2 - (i_{10} + i_{20})X_1X_2}{d_0^2X_1 + (1-d_0)^2X_2 + j\omega C_C X_1X_2} \end{aligned} \quad (12)$$

$$\begin{aligned} H_d &= \frac{d_1}{v_{C1}} \\ &= \frac{(1-d_0) \left(1 - \frac{d_0 T}{2L_1} r_1 \right) X_2 + \frac{d_0 T}{2L_2} X_1X_2 - d_0X_3}{\Gamma} \end{aligned} \quad (13)$$

where

$$\begin{aligned} \Gamma &= \left(1 - \frac{d_0 T}{2L_1} r_1 \right) v_{C0}X_2 + v_{C0}X_3 + I_{\text{comp}}X_1X_2 \\ &\quad + \frac{T}{2} \left(\frac{E - i_{10}r_1}{L_1} + \frac{v_{C0} - i_{20}(R+r_2)}{L_2} \right) X_1X_2 \end{aligned}$$

along with $X_1 = r_1 + j\omega L_1$, $X_2 = r_2 + j\omega L_2 + (R)/(1 + j\omega C_O R)$ and $X_3 = X_1[1 - (d_0 T)/(2L_2)(r_2 + (R)/(1 + j\omega C_O R))]$. The loop gain of the system is therefore obtained as

$$H_{\text{loop}} = H_{v_C} H_d. \quad (14)$$

Equation (14) allows us to find the slow-scale bifurcation boundary numerically in the parameter space according to the

Fig. 8. Stability boundaries for different values of damping resistance: upper line for $r_1 = 0.73 \Omega$, middle line for $r_1 = 0.53 \Omega$, and bottom line for $r_1 = 0.33 \Omega$. Points are boundaries found from full-circuit simulations. Unstable and stable regions of operation are located above and below the line, respectively.

Fig. 9. Stability boundaries for different values of capacitance: upper line for $C_C = 1.5 \mu\text{F}$, middle line for $C_C = 1.0 \mu\text{F}$, and bottom line for $C_C = 0.5 \mu\text{F}$. Points are boundaries found from full-circuit simulations. Unstable and stable regions of operation are located above and below the line, respectively.

Barkhausen criteria, i.e., $\angle H_{\text{loop}}(\omega) = 0$ and $|H_{\text{loop}}(\omega)| = 1$ for some $\omega > 0$.

It should be noted that the Barkhausen criteria do not generally give necessary and sufficient conditions for oscillations. Here, as oscillation is known to exist, the Barkhausen criteria can be conveniently used to find the conditions for oscillation.

V. STABILITY BOUNDARIES

Of practical interest is the condition under which the system may exhibit slow-scale oscillations. Using (14), we may plot the stability boundaries for different values of R, r_1 and C_C or for virtually any choice of parameter space. Figs. 7–9 show the specific stability boundaries corresponding to the choice of component values given in Tables I and II. Also shown in the figures are points on the stability boundaries obtained from full-

circuit simulations. The excellent agreement between analysis and the full-circuit simulations clearly proves the ability of the loop-gain analysis in explaining the current loop-induced slow-scale bifurcations.

VI. CONCLUSION

A current-mode controlled Ćuk converter has been studied in this paper. For current-mode controlled simple low-order dc–dc converters, it has been commonly known that slow-scale bifurcation is caused by parameter changes of the outer voltage loop, while fast-scale bifurcation is due to the fast inner current loop. In this paper, we have demonstrated that, for higher order converters under a similar current-mode control, however, the inner current loop can induce slow-scale bifurcation in the absence of a closed outer voltage loop. The phenomenon has been analyzed using an averaged model in terms of the closed-loop stability of the inner current loop of the system. In conclusion, the extra degrees of freedom in higher order dc–dc converters have opened up a new possible mode of instability which has not been found in simple low-order dc–dc converters. In the case of the current-mode controlled Ćuk converter, slow-scale instability becomes possible even without a closed outer voltage loop.

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